

Show no work. **NOTE:** Write **DNE** in a blank if the described object does not exist or if the indicated operation cannot be performed. Do **not** approx.: If your result is “ $\sin(\sqrt{\pi})$ ” then write that rather than $.9797\cdots$.

D1:

[z] A series $\sum_{k=3}^{\infty} a_k$ is *absolutely convergent* if

..... An example of an \mathbb{R} -convergent series
..... that is not abs.conv, has k^{th} term $a_k :=$

[a] One lobe of polar-curve $r = 6 \cdot \cos(3\theta)$, has area

$$\int_{\dots}^{\dots} \left[\dots \right] \cdot d\theta.$$

[b] $\sum_{k=5}^{50} 8^k = \frac{N}{D}$, where $N =$, $D =$

[c] Let $b_n := e^{4/[n+5]}$ note $\exp(\frac{4}{n+5})$. Then

$$\sum_{n=3}^{\infty} [b_n - b_{n+1}] = \dots$$

[Hint: A real, $+\infty$, $-\infty$ or **DNE** in \mathbb{R} .]

[d] The Mac of $\frac{4 \cdot x}{2 + x^2}$ has RoC=

Mac(x)=

.....
Write the first 5 non-zero terms, e.g, $8x^3 + \frac{1}{8}x^6 + \frac{3}{2}x^8 - x^{12} - 7x^{15} + \cdots$.

D2: “Water” on planet *Light* has density $7 \frac{\text{lb}}{\text{ft}^3}$. A dam $\mathbf{T} = \mathbf{T}_B$, in form of an isosceles trapezoid, has base width B :: ft, top width $50\text{ft} + B$ (of the parallel edge), and slant-height 65ft . So H :=

(an)

(integer) is the dam’s height. In terms of H, B and 50ft ,

Area(\mathbf{T})=

Geometrically, $\lim_{B \nearrow \infty} Y_B =$

where Y_B note

.....
denotes how far Centroid(\mathbf{T}) lies below Top(\mathbf{T}).

Water comes just to the top of \mathbf{T} . Hence the total hydrostatic force on \mathbf{T} is (IToF $H, B, 50\text{ft}$ and $7\text{lb}/\text{ft}^3$)

$$F_B := \left[\dots \right] \cdot \text{lb.}$$

D1: _____ 220pts

D2: _____ 75pts

Total: _____ 295pts

HONOR CODE: *“I have neither requested nor received help on this exam other than from my professor (or his colleague).”*
Name/Signature/Ord