

Sets and Logic
MHF3202 17HE

Class-B

Prof. JLF King
Wednesday, 26Oct2022

B4: Short answer. Show no work. Write LARGE.

Write **DNE** if the object does not exist or the operation cannot be performed. NB: **DNE** $\neq \{\}$ $\neq 0$.

a For a LOR (letter-of-recommendation), Prof. K requires two courses, or a Special Topics or graduate course Circle:

Yes

True

Darn tootin'!

b Mimicking what we did in class: From the 987×200 game-board, cut-out (remove) the (35, 150)-cell and one other cell at $P = (x, y)$. Circle those choices for P ,

(150, 160), (14, 35), (66, 77), (195, 15), (123, 4)

which, if removed, would leave a board that *definitely* cannot be domino-tiled.

c Both \sim and \bowtie are equiv-relations on a set Ω . Define binrels **I** and **U** on Ω as follows.

Define $\omega \mathbf{U} \lambda$ IFF *Either* $\omega \sim \lambda$ *or* $\omega \bowtie \lambda$ [or both].

Define $\omega \mathbf{I} \lambda$ IFF *Both* $\omega \sim \lambda$ *and* $\omega \bowtie \lambda$.

So “**U** is an equiv-relation” is:

T F

So “**I** is an equiv-relation” is:

T F

d Let δ_N be the number of derangements of $[1..N]$, and $P_N := \frac{\delta_N}{N!}$ the probability that an N -perm is a derangement. Written in Incl-Excl notation (the formula we derived in class), $\delta_{17} =$

Limit $\left[\lim_{N \rightarrow \infty} P_N \right]$ equals _____.

e On a 4-set, there are _____ many equivalence relations.

f Let \mathcal{P}_∞ denote the family of all *infinite* subsets of \mathbb{N} . Define relation \approx on \mathcal{P}_∞ by: $A \approx B$ IFF $A \cap B$ is infinite. Stmt “*This \approx is an equivalence-relation*” is: T F

OYOP: In *grammatical English sentences*, write your essay on every 2nd line (usually), so I can easily write between the lines.

B5: Consider a strict well-order \prec on set \mathbf{U} , and a strict well-order $<$ on Γ . Define binrel \ll on $\mathbf{U} \times \Gamma$ by:

$$(b, \alpha) \ll (c, \beta)$$

IFF *Either* $b \prec c$ *or* $[b = c \text{ and } \alpha < \beta]$.

Prove: *Relation \ll is a well-order on $\mathbf{U} \times \Gamma$.*

B4: _____ 105pts

B5: _____ 40pts

Total: _____ 145pts

NAME:

HONOR CODE: “*I have neither requested nor received help on this exam other than from my professor or TA.*”

Signature:
