

PRACTICE: Binomials, C-arithmetic

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Welcome. [This is not a practice exam; just some practice problems.] Note: **ITO**=In-Terms-Of.

Our first exam will be on Wednesday, 03Feb2021, during classtime, via Canvas.

P1:

a Values $[\pi \uparrow 3] = \dots$ and $[\frac{5}{3} \downarrow 4] = \dots$

b Binomial coefficient $\binom{7}{4} = \dots = \dots$

c Multinomial coefficient $\binom{9}{4, 2, 3} = \dots = \dots$

[Note: Write your ans. ITO of factorials, then **also** write it as a single integer, or product of two, **without** factorials.]

d In $[5x^2 + 4y + z^3 + 7]^{20}$, compute these coeffs:
 Coeff($x^6 z^8$) = \dots
 Coeff($y^5 z^6$) = \dots

[You may write answers as a product numbers, powers and multinomial-coeffs.]

P2:

e $[\sqrt{5}]^{\sqrt{2}}]^{\sqrt{8}} = \dots$; $\log_8(4) = \dots$

f Blanks $\in \mathbb{R}$. So $\frac{1}{2+3i} = \dots + i \cdot [\dots]$.

Thus $\text{Im}\left(\frac{5-i}{2+3i}\right) = \dots$

By the way, $|5-3i| = \dots$

g Let $A := 2+i$, $B := 1-i$, $P := 5$, $Q := 3i$, $\alpha := 1$ and $\beta := 1+3i$. Complex numbers w and z satisfy

$$\begin{aligned} Aw + Bz &= \alpha \quad \text{and} \\ Pw + Qz &= \beta. \end{aligned}$$

Then $w = \dots$

h Reals $x = \dots$ and $y = \dots$

where $x + iy = [1+i]^{86}$. [Hint: Multiplying complexes multiplies their moduli, and adds their angles.]

i Complex number $[x + iy]^2 = -8i$, for real numbers $x > y$, where $x = \dots$ and $y = \dots$

j Number $6 \cdot \exp\left(i \cdot \frac{5\pi}{3}\right)$ equals $x + yi$ for reals $x = \dots$ and $y = \dots$

With $v := \exp(-2 + 5i)$, then $|v| = \dots$

And $|v|$ lies in circle the correct interval

$(0, \frac{1}{2})$, $[\frac{1}{2}, 1)$, $[1, 2)$, $[2, 4)$, $[4, 8)$, $[8, \infty)$.