

Show no work. *NOTE:* Write **DNE** in a blank if the described object does not exist or if the indicated operation cannot be performed. Do **not** approx.: If your result is “sin(√π)” then write that rather than .9797... .

**D1:**                220pts

**D2:**                75pts

**Total:**                295pts

**D1:**

**z** A series  $\sum_{k=3}^{\infty} a_k$  is **absolutely convergent** if

.....  
 ..... An example of an  $\mathbb{R}$ -convergent series  
 .....  
 that is **not** abs.conv, has  $k^{\text{th}}$  term  $a_k :=$  .....

**HONOR CODE:** “I have neither requested nor received help on this exam other than from my professor (or his colleague).”  
*Name/Signature/Ord*

**a** One lobe of polar-curve  $r = 6 \cdot \cos(3\theta)$ , has area

$$\int \left[ \dots \right] \cdot d\theta.$$

Ord: .....

**b**  $\sum_{k=5}^{50} 8^k = \frac{N}{D}$ , where  $N =$  .....,  $D =$  .....

**c** Let  $b_n := e^{4/[n+5]}$  note  $\exp\left(\frac{4}{n+5}\right)$ . Then

$$\sum_{n=3}^{\infty} [b_n - b_{n+1}] =$$

.....  
 [Hint: A real,  $+\infty$ ,  $-\infty$  or **DNEin** $\mathbb{R}$ .]

**d** The Mac of  $\frac{4 \cdot x}{2 + x^2}$  has RoC= .....

Mac(x)= .....

Write the first 5 non-zero terms, e.g,  $8x^3 + \frac{1}{8}x^6 + \frac{3}{2}x^8 - x^{12} - 7x^{15} + \dots$ .

**D2:** “Water” on planet *Light* has density  $7 \frac{\text{lb}}{\text{ft}^3}$ . A dam  $\mathbf{T} = \mathbf{T}_B$ , in form of an isosceles trapezoid, has base width  $B :: \text{ft}$ , top width  $50\text{ft} + B$  (of the parallel edge), and slant-height  $65\text{ft}$ . So  $H :=$

(an integer) is the dam’s height. In terms of  $H, B$  and  $50\text{ft}$ ,

Area( $\mathbf{T}$ )= ..... [Verified units?]

Geometrically,  $\lim_{B \nearrow \infty} Y_B =$  ..... and  $Y_0 =$  .....

where  $Y_B$  note

denotes how far Centroid( $\mathbf{T}$ ) lies *below* Top( $\mathbf{T}$ ).

Water comes just to the top of  $\mathbf{T}$ . Hence the total hydrostatic force on  $\mathbf{T}$  is (ITOf  $H, B, 50\text{ft}$  and  $7\text{lb}/\text{ft}^3$ )

$$F_B := \left[ \dots \right] \cdot \text{lb.}$$