

**Hello.** Please write **DNE** in a blank if the described object does not exist or if the indicated operation cannot be performed. **Write expressions unambiguously e.g., “ $1/a + b$ ” should be bracketed either  $[1/a] + b$  or  $1/[a + b]$ . (Be careful with negative signs!)**

Do **not** approx.: If your result is “ $\sin(\sqrt{\pi})$ ” then write that rather than .9797...

Use “ $f(x)$  notation” when writing fncs; in particular, for trig and log fncs. E.g, write “ $\sin(x)$ ” rather than the horrible  $\sin x$  or  $[\sin x]$ .

Write *rational numbers* as fractions: E.g  $\frac{1}{2}$  and  $1/3$ , but not 0.5 nor 0.3333...; **use fractions.**

**A4:** Show no work.

**a** Fnc  $y_\beta(t) :=$  \_\_\_\_\_

is the general soln to  $\frac{dy}{dt} = 8t^3 \cdot [y - 5]$ . [Hint: SoV.]

The *particular*  $y()$  with  $y(0) = 8$  is  $y(t) :=$  \_\_\_\_\_ . And this

function has  $y(1) =$  \_\_\_\_\_ .

**b** Function  $h()$  satisfies  $2h'' + h' - 6h = 0$ , and initial conditions  $h(0) = 5$  and  $h'(0) = -3$ . So

$$h(t) = \alpha e^{At} + \beta e^{Bt}, \text{ for numbers}$$

$$\alpha = \text{_____}, A = \text{_____}, \beta = \text{_____}, B = \text{_____}.$$

**c** Fnc  $y_\alpha(t) :=$  \_\_\_\_\_

is the general soln to  $y' + \left[\frac{2}{t} \cdot y\right] = t^3$ . [Hint: FOLDE.]

**A5:** Show no work.

**d** DiffOperators **P, Q, R, S** are defined as

$$\begin{aligned} \mathbf{P}(f) &:= f(3) \cdot f', & \mathbf{Q}(f) &:= \cos(3) \cdot f^{(3)}, \\ \mathbf{R}(f) &:= [\cos(3) \cdot f] + f'', & \mathbf{S}(f) &:= \cos(3) + [3f']. \end{aligned}$$

Then... **P** is linear:  $T$   $F$ .      **Q** is linear:  $T$   $F$ .  
**R** is linear:  $T$   $F$ .                      **S** is linear:  $T$   $F$ .

**e** The discriminant of polynomial  $f(x) := 3x^2 + 3x + 1$  is  $\text{Discr}(f) =$  \_\_\_\_\_.

**f** Blanks  $\in \mathbb{R}$ . So  $\frac{1}{1-3i} =$  \_\_\_\_\_  $+ i \cdot$  \_\_\_\_\_.

Thus  $\frac{-2 + 5i}{1 - 3i} =$  \_\_\_\_\_  $+ i \cdot$  \_\_\_\_\_.

By the way,  $|-4 + 5i| =$  \_\_\_\_\_.

End of A-Class

**A4:** \_\_\_\_\_ 120pts

**A5:** \_\_\_\_\_ 65pts

**Total:** \_\_\_\_\_ 185pts