

**A1:**     \_\_\_ \_\_\_     35pts

**A2:**     \_\_\_ \_\_\_ \_\_\_     100pts

**A3:**     \_\_\_ \_\_\_     20pts

Essay not  
double-spaced:     \_\_\_ \_\_\_     -15pts

**Total:**     \_\_\_ \_\_\_ \_\_\_     155pts

*In complete English sentences on your own sheets of paper, please write, double-spaced, this proof. Do not restate the problem.*

**A1:** Prove that the set of primes is infinite. [Euclid's theorem]

**A2:** *Show no work. Please write DNE in a blank if the described object does not exist or if the indicated operation cannot be performed.*

**a** Euler  $\varphi(121000) =$  \_\_\_\_\_ .  
Express your answer as a product  $p_1^{e_1} \cdot p_2^{e_2} \cdot \dots$  of primes to posit powers, with  $p_1 < p_2 < \dots$

**b** LBolt gives  $G := \text{Gcd}(413, 294) =$  \_\_\_\_\_ . And  $413S + 294T = G$ , where  $S =$  \_\_\_\_\_ &  $T =$  \_\_\_\_\_ are integers.

**c** Since  $4800 = 2^6 \cdot 3^1 \cdot 5^2$ , it has \_\_\_\_\_ many positive divisors. [Write ANS naturally as a product of integers.]

**d**  $[\sqrt{3}^{\sqrt{2}}]^{\sqrt{8}} =$  \_\_\_\_\_ .  $\log_8(4) =$  \_\_\_\_\_ .

**e** Compute the sum of this geometric series:  
 $\sum_{n=1}^{\infty} [-1]^n \cdot [3/5]^n =$  \_\_\_\_\_ .

**A3: Math-Greek alphabet:** Please write the two missing data of lowercase/upercase/name. Eg:

“iota:      $\alpha$ :     B:     .” You fill in:  $\iota$  I A alpha  $\beta$  beta

$\Omega$ :     \_\_\_\_\_      $\Lambda$ :     \_\_\_\_\_      $\Gamma$ :     \_\_\_\_\_

$\xi$ :     \_\_\_\_\_      $\sigma$ :     \_\_\_\_\_      $\eta$ :     \_\_\_\_\_

rho     theta     zeta     mu